Figure 13.A. The Production Function

| Number of <br> Workers | Total <br> Product (TP) | Marginal <br> Product | Average <br> Product |  |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | $--\ldots------$ | ---------- |  |
| 1 | 5 | $5-0=5$ | $5 / 1=5$ | Stage I |
| 2 | 30 | $20-5=15$ | $15 / 2=7.5$ |  |
| 3 | 35 | $35-30=5$ | $35 / 4=8.75$ |  |
| 4 | 32 | $32-35=-3$ | $32 / 5=6.4$ | Stage II |
| 5 |  |  | $30 / 3=10$ |  |

Figure 13.B. The Production Function


Figure 13.C. The Production Function for Oklahoma Wheat

| lbs Nitrogen Per Acre | Wheat Yield (Total Product) bushels / acre | Marginal Product of Nitrogen | Average Product of Nitrogen |
| :---: | :---: | :---: | :---: |
| 0 | 23.0 | ----------------------------- | ---------------------------- |
| 20 | 30.5 | $(30.5-23.0) /(20-0)=0.375$ | $32 / 20=1.525$ |
| 40 | 35.0 | $(35.0-30.5) /(40-20)=0.225$ | $37 / 40=0.875$ |
| 60 | 37.0 | $(37.0-35.0) /(60-40)=0.100$ | $40 / 60=0.617$ |
| 80 | 37.8 | $(37.8-37.0) /(80-60)=0.040$ | $43 / 80=0.473$ |

Figure 13.D. Marginal Value and Cost of Input Use

| lbs Nitrogen Per Acre | Wheat <br> Yield <br> (Total <br> Product) <br> bushels / acre | Marginal Product of Nitrogen bushels / acre | Average Product of Nitrogen bushels / acre | Marginal Value of Nitrogen (Wheat Price = \$3.25 / bu) \$ / acre | Marginal Cost of Nitrogen (Nitrogen Price = \$0.15 / lb N) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 23.0 | ---------- | ---------- | ---- | ---------- |
| 20 | 30.5 | 0.375 | 1.53 | $\begin{array}{r} 0.375 * 3.25 \\ =\$ 1.22 \end{array}$ | \$0.15 |
| 40 | 35.0 | 0.225 | 0.88 | \$0.73 | \$0.15 |
| 60 | 37.0 | 0.100 | 0.62 | \$0.33 | \$0.15 |
| 80 | 37.8 | 0.040 | 0.47 | \$0.13 | \$0.15 |

Figure 13.E. Solving for the Optimal Number of Days on Feed
Set Marginal Value of Input = Input Price
Assume output price $=P_{L C}=0.75$; Input Price $=p_{D O F}=1.41$

$$
\begin{gathered}
P_{L C}\left[4.36-0.0157\left(\mathrm{DOF}^{*}\right)\right]=p_{D O F} \\
0.75\left[4.36-0.0157\left(\mathrm{DOF}^{*}\right)\right]=1.41 \\
\mathrm{DOF}^{*}=(3.27-1.41) / 0.013775=158 \text { days on feed }
\end{gathered}
$$




An increase (decrease) in the input price decreases (increases) input use by the firm.
An increase (decrease) in marginal product or output price increases (decreases) input use by the firm.


Figure 13.G. Marginal and Average Cost Curves


Figure 13.H. Marginal and Average Cost Curves


Figure 13.I. Hypothetical Firm (cost per worker $=\$ 10$; fixed costs $=$ \$15)

| Number <br> of <br> Workers | Total <br> Product <br> (TP) | Variable <br> Costs | Fixed <br> Cost | Total <br> Costs | Marginal <br> Cost | Average Variable <br> Cost | Average Cost |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | $\$ 0$ | $\$ 15$ | $\$ 15$ | ------- | $---\cdots---$ | ------- |
| 1 | 5 | $\$ 10$ | $\$ 15$ | $\$ 25$ | $(\$ 25-\$ 15) /$ <br> $\$(5-0)=\$ 2$ | $\$ 10 / 5=\$ 2$ | $\$ 5$ |
| 2 | 20 | $\$ 20$ | $\$ 15$ | $\$ 35$ | $\$ 0.66$ | $\$ 1$ | $\$ 1.75$ |
| 3 | 30 | $\$ 30$ | $\$ 15$ | $\$ 45$ | $\$ 1$ | $\$ 1$ | $\$ 1.5$ |
| 4 | 35 | $\$ 40$ | $\$ 15$ | $\$ 55$ | $\$ 2$ | $\$ 1.14$ | $\$ 1.57$ |
| 5 | 32 | $\$ 50$ | $\$ 15$ | $\$ 65$ | --------- | $\$ 1.56$ | $\$ 2.03$ |



Figure 13.J. The Firm's Production Decision


Figure 13.K. Firm Costs in the Long-Run


Figure 13.L. Economies of Scale and Number of Brewers in the U.S. Brewing Industry

| Year | Minimum <br> Efficient Scale <br> (millions of <br> barrels) | Number of <br> Mass- <br> Producing <br> Brewing <br> Companies |
| :---: | ---: | ---: |
| 1950 | 0.1 | 350 |
| 1970 | 8.0 | 75 |
| 2000 | 18.0 | 24 |

Source: Tremblay and Tremblay

